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Non-uniqueness of solutions of a semilinear heat equation with singular initial data

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We construct new examples of non-uniqueness of positive solutions of the Cauchy problem for the Fujita equation. The solutions we find are not self-similar and some of them blow up in finite time. Connecting orbits and ancient solutions of a rescaled equation play a key role in our constructions.